

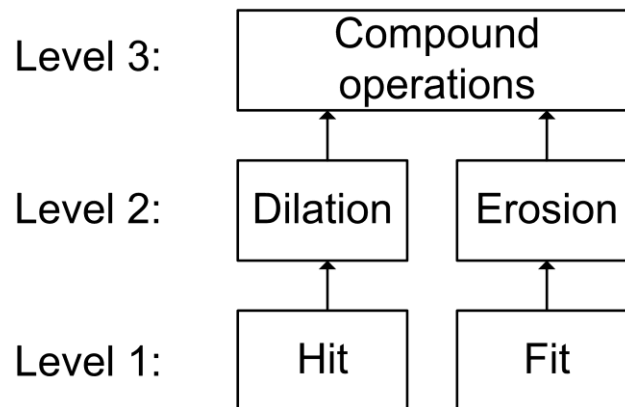


# Morfologi Citra

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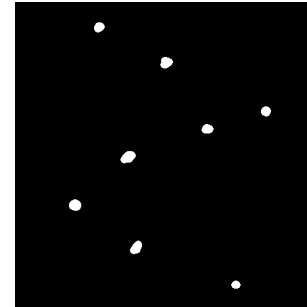
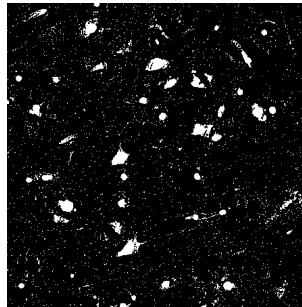
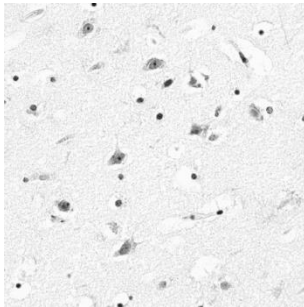
# Morfologi Citra

- Apa yang bisa dilakukan oleh morfologi citra ?
- Operasi morfologi :
  - Fit dan Hit
  - Erosi (Erosion)
  - Dilasi (Dilation)
  - Operasi Gabungan (Compound Operations)

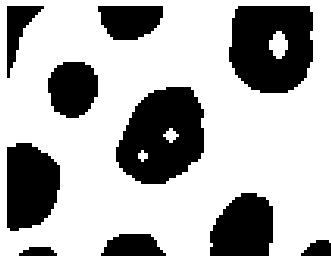


# Kegunaan Morfologi

- Remove Noise
  - Small Objects

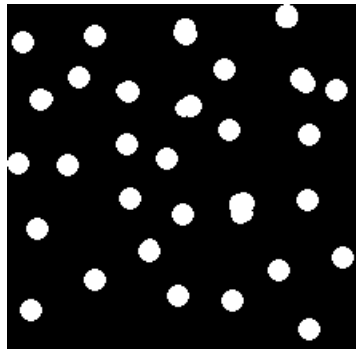
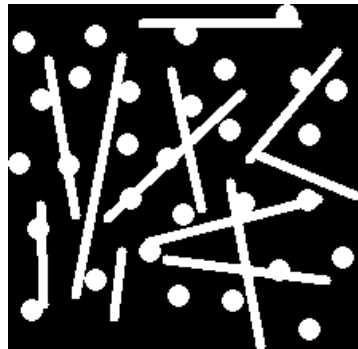
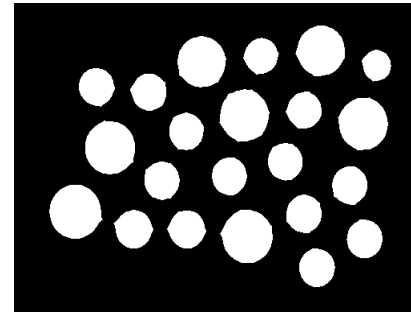
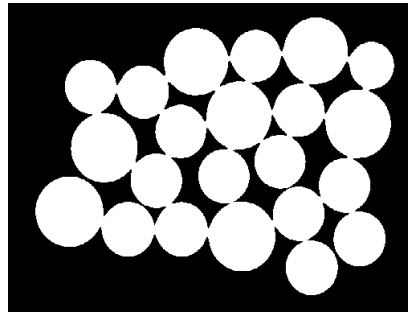
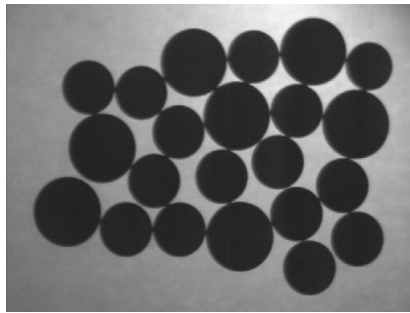


- Fill holes



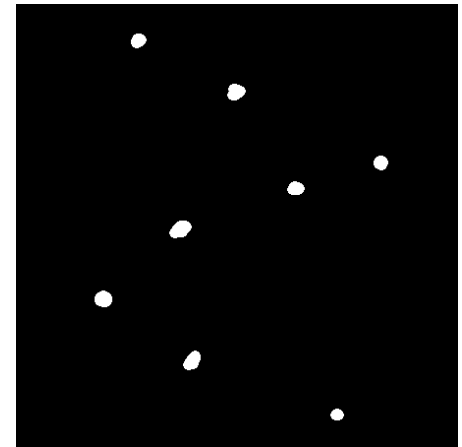
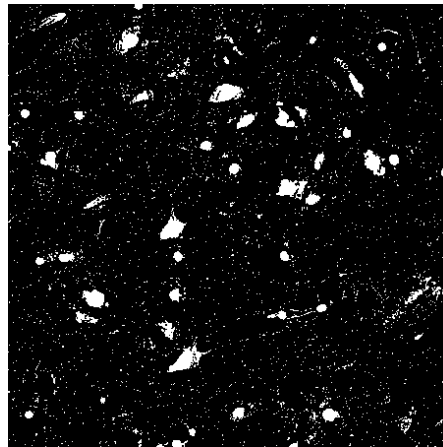
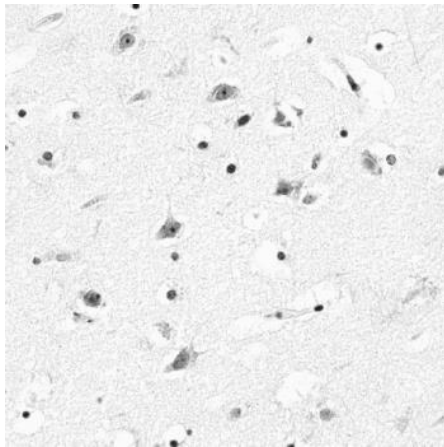
# Kegunaan Morfologi

- Isolate Objects



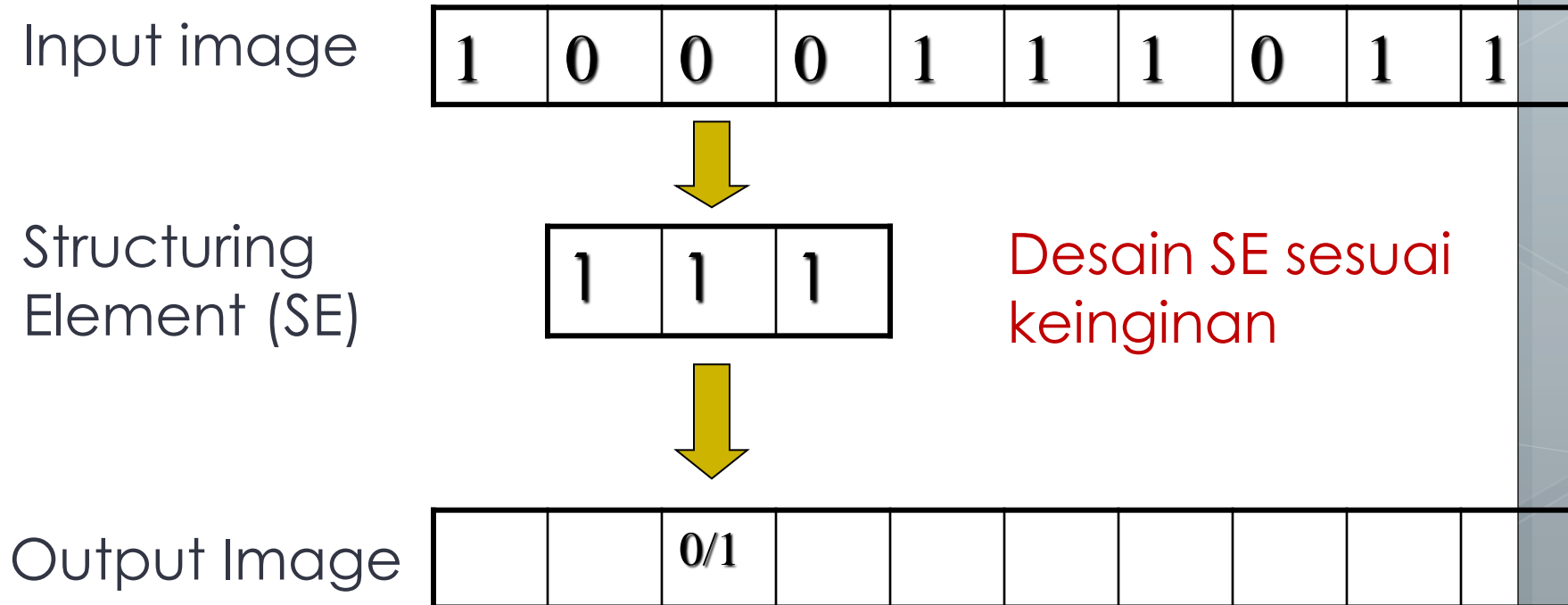
# Cara Kerja Morfologi Citra

- Konversi citra ke dalam bentuk Grayscale
- Lakukan binerisasi citra → Thresholding
- Morfologi



- Dapat juga diterapkan pada citra grayscale

## Hit dan Fit untuk Citra 1D



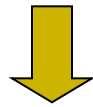
**Hit:** If just one of the '1's in the SE match with the input =>  
output = 1, otherwise output = 0

**Fit:** If all '1's in the SE match with input =>  
output = 1, otherwise output = 0

# Dilasi (Dilation) berdasarkan Operasi Hit

Input image

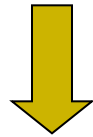
1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring  
Element (SE)

1	1	1
---	---	---

$$g(x) = f(x) \oplus SE$$



Output Image

	1								
--	---	--	--	--	--	--	--	--	--

**Hit:** If just one of the '1's in the SE match with the input =>  
output = 1, otherwise output = 0

# Contoh Dilasi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	1	0							
--	---	---	--	--	--	--	--	--	--



# Contoh Dilasi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	1	0	1						
--	---	---	---	--	--	--	--	--	--

# Contoh Dilasi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	1	0	1	1					
--	---	---	---	---	--	--	--	--	--

# Contoh Dilasi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	1	0	1	1	1				
--	---	---	---	---	---	--	--	--	--

# Contoh Dilasi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	1	0	1	1	1	1			
--	---	---	---	---	---	---	--	--	--

# Contoh Dilasi

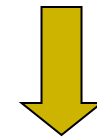
Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output


	1	0	1	1	1	1	1		
--	---	---	---	---	---	---	---	--	--

## Contoh Dilasi

Input


1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

SE



1	1	1
---	---	---

Output



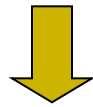
	1	0	1	1	1	1	1	1	
--	---	---	---	---	---	---	---	---	--

**Object (1) menjadi lebih besar dan holes (0) menjadi terisi dengan object atau hilang**

# Erosi (Erosion) berdasarkan Operasi Fit

Input image

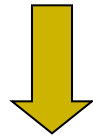
1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



Structuring  
Element (SE)

1	1	1
---	---	---

$$g(x) = f(x) \ominus SE$$



Output Image

	0								
--	---	--	--	--	--	--	--	--	--

**Fit: If all '1's in the SE match with input =>  
output = 1, otherwise output = 0**

# Contoh Erosi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	0	0							
--	---	---	--	--	--	--	--	--	--



# Contoh Erosi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	0	0	0						
--	---	---	---	--	--	--	--	--	--

# Contoh Erosi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	0	0	0	0					
--	---	---	---	---	--	--	--	--	--

# Contoh Erosi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

	0	0	0	0	1				
--	---	---	---	---	---	--	--	--	--

# Contoh Erosi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---



SE

1	1	1
---	---	---



Output

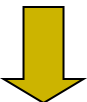
	0	0	0	0	1	0			
--	---	---	---	---	---	---	--	--	--

# Contoh Erosi

Input


1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

SE



1	1	1
---	---	---

Output



	0	0	0	0	1	0	0		
--	---	---	---	---	---	---	---	--	--

## Contoh Erosi

Input

1	0	0	0	1	1	1	0	1	1
---	---	---	---	---	---	---	---	---	---

SE

1	1	1
---	---	---

Output

	0	0	0	0	1	0	0	0	
--	---	---	---	---	---	---	---	---	--

**Object (1) menjadi lebih kecil**

# Morfologi Citra

- Structuring Elements (SE) dapat terdiri dari sebarang ukuran sesuai dengan kebutuhan
- Nilai dari elemen adalah **0** atau **1**, namun dimungkinkan memiliki nilai yang lain (termasuk tidak ada nilainya)
- Nilai kosong pada SE berarti bebas (*don't care*)

Box →

1	1	1
1	1	1
1	1	1

Disc ↘

	1	
1	1	1
	1	

		1	1	1		
	1	1	1	1	1	
1	1	1	1	1	1	1
1	1	1	1	1	1	1
	1	1	1	1	1	
		1	1	1		

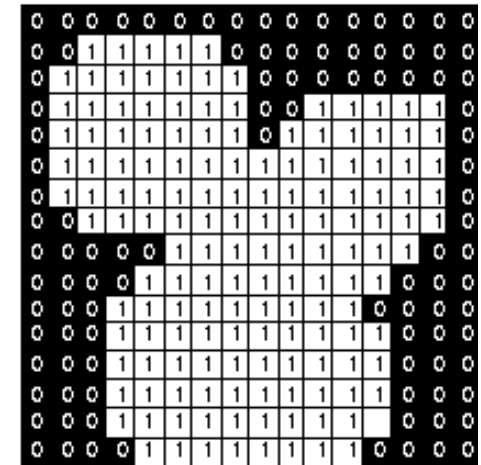
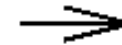
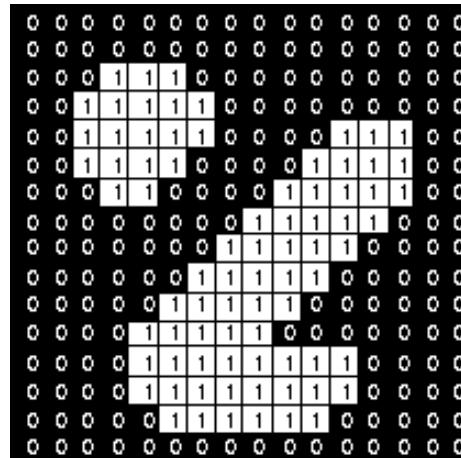
1	1	
1	0	
1		0

# Dilasi (2-Dimensi) ← Hit

$$g(x, y) = f(x, y) \oplus SE$$

Structuring  
Element

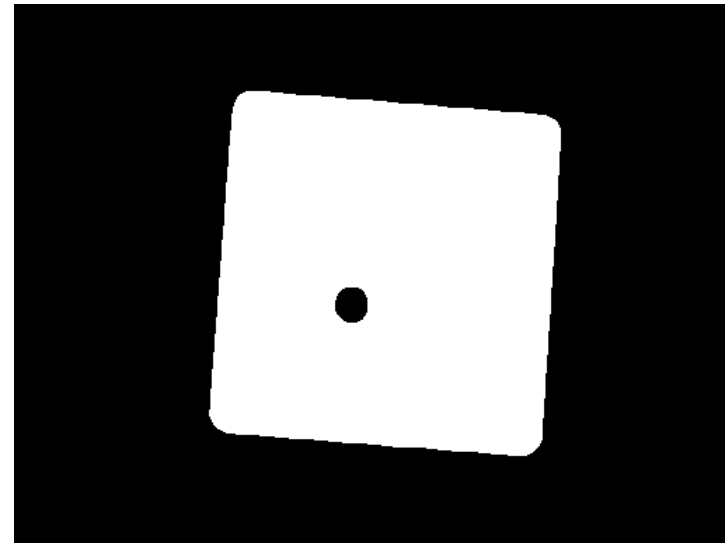
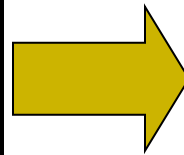
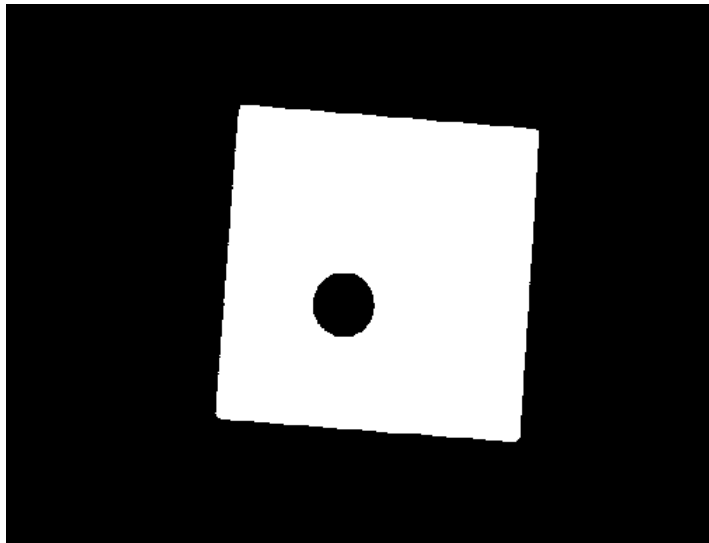
1	1	1
1	1	1
1	1	1



- Objects tergabung (holes terisi object)
- Sudut yang tajam dihaluskan



# Contoh Dilasi



		1	1	1		
	1	1	1	1	1	
1	1	1	1	1	1	1
1	1	1	1	1	1	1
1	1	1	1	1	1	1
	1	1	1	1	1	
		1	1	1		

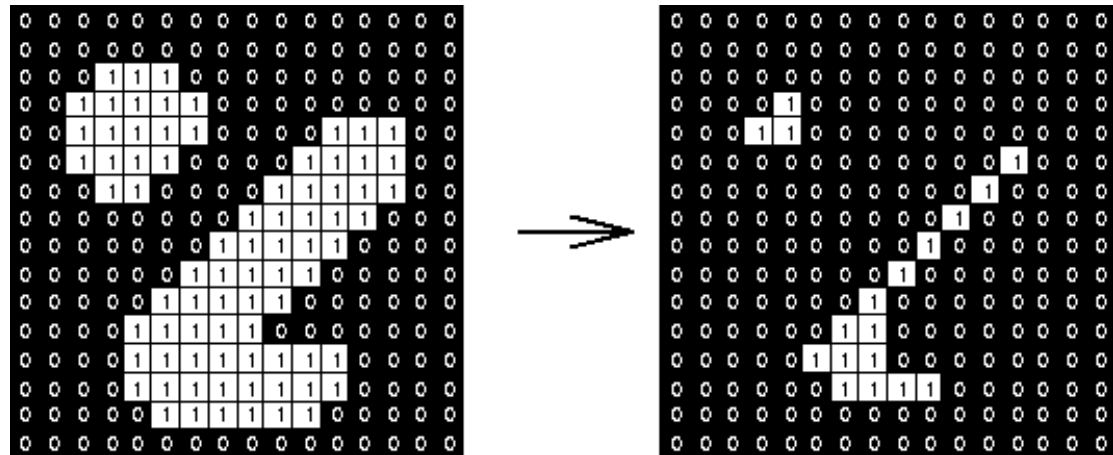
Structuring element:  
disc => rounded corners

# Erosi (2-Dimensi) ← Fit

$$g(x, y) = f(x, y) \ominus SE$$

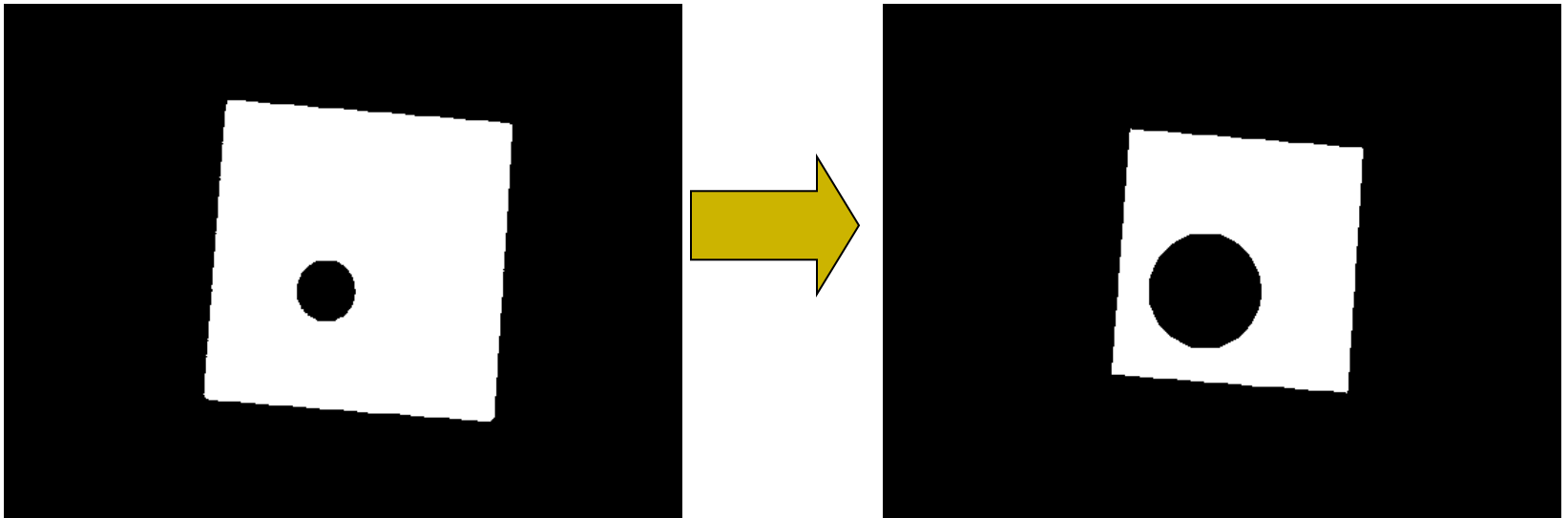
Structuring  
Element

1	1	1
1	1	1
1	1	1



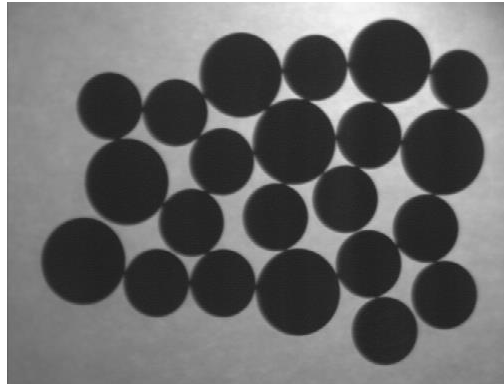
- Objects menjadi lebih kecil

# Contoh Erosi

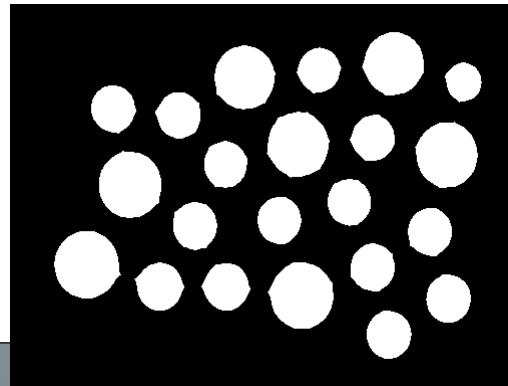
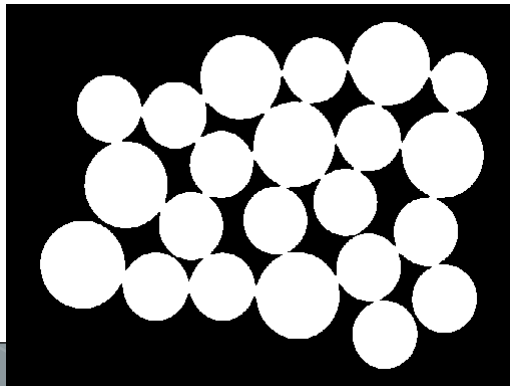


# Aplikasi Menghitung Koin

- Kesulitan menghitung koin pada gambar di bawah disebabkan tergabungnya object koin



- Solusi: Thresholding dan Erosi utk memisahkannya!

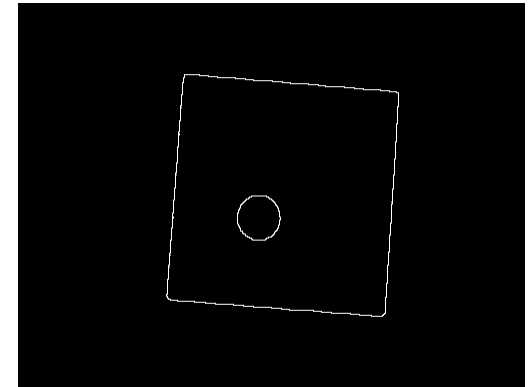
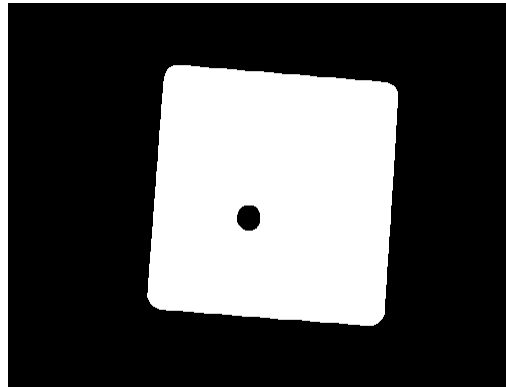
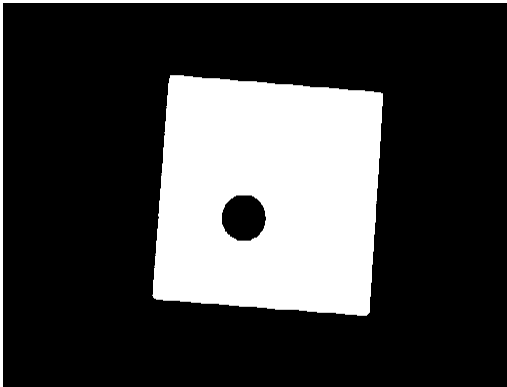


# Compound Operations

- Menggabungkan operasi Erosion dan Dilation kedalam level operasi yang lebih tinggi (more advanced)
  - Mencari garis tepi (*outline*)
  - *Opening*: mengisolasi objects dan menghilangkan object-object kecil (lebih baik daripada Erosion)
  - *Closing*: mengisi holes pada citra (lebih baik daripada Dilation)

## Mencari garis tepi (outline)

- Operasi Dilasi (object menjadi lebih besar)
- Substraksi citra asal dengan citra hasil dilasi
- Didapatkan outline



# Opening

- Motivasi: menghilangkan object-object kecil  
TETAPI tetap mempertahankan ukuran aslinya
- Opening = Erosion + Dilation
  - Gunakan SE yang sama
  - Hampir sama dengan erosi tetapi tidak terlalu *destructive*
- Math:

$$f(x, y) \circ SE = (f(x, y) \ominus SE) \oplus SE$$

- Opening adalah *idempotent*: operasi opening yang diulang-ulang tidak memberikan dampak yang berkelanjutan!

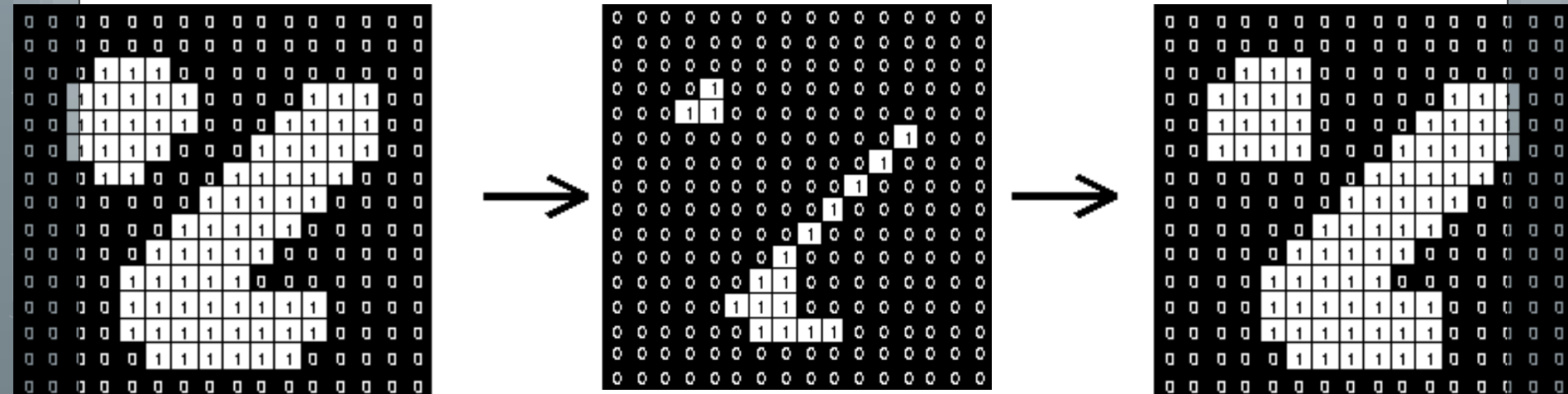
# Contoh Opening

SE

1	1	1
1	1	1
1	1	1

Erosion

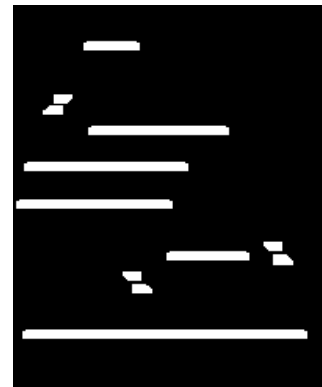
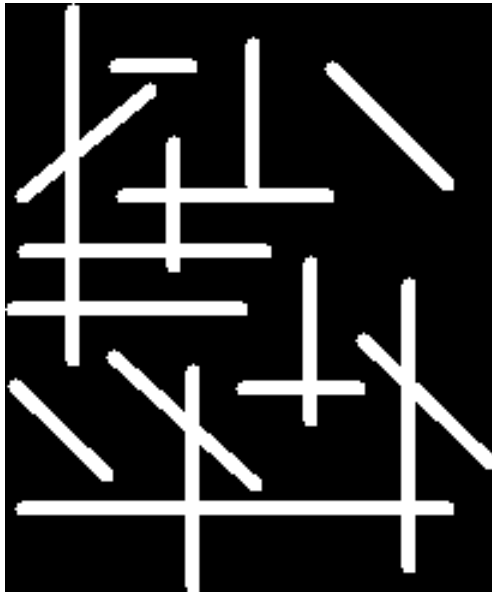
Dilation





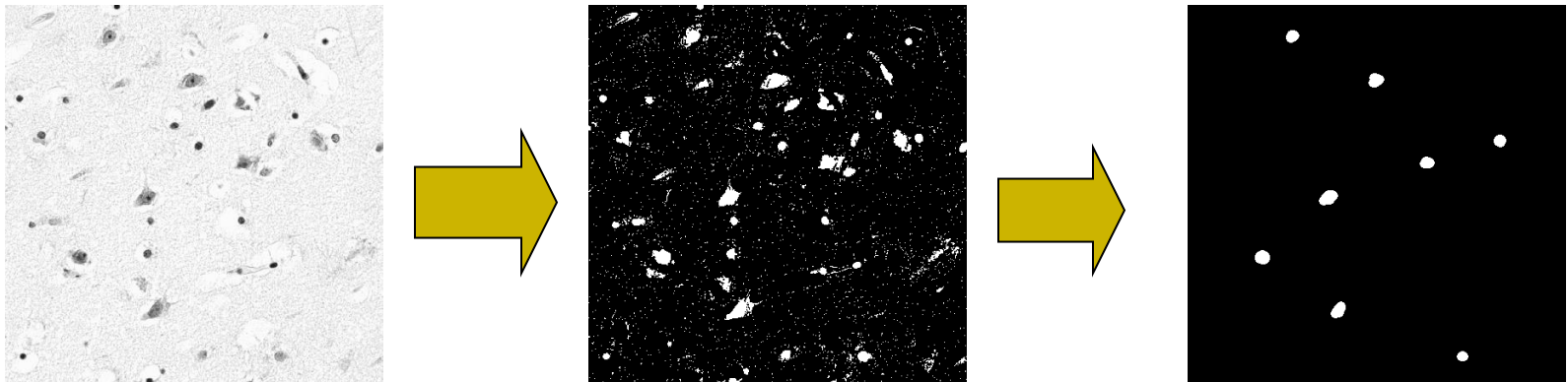
# Contoh Opening

- 9x3 and 3x9 Structuring Elements



# Contoh Opening

- Structuring Element: 11 pixel disc



(show: cell\_colony, 3 x erosion, 3 x dilation)

# Closing

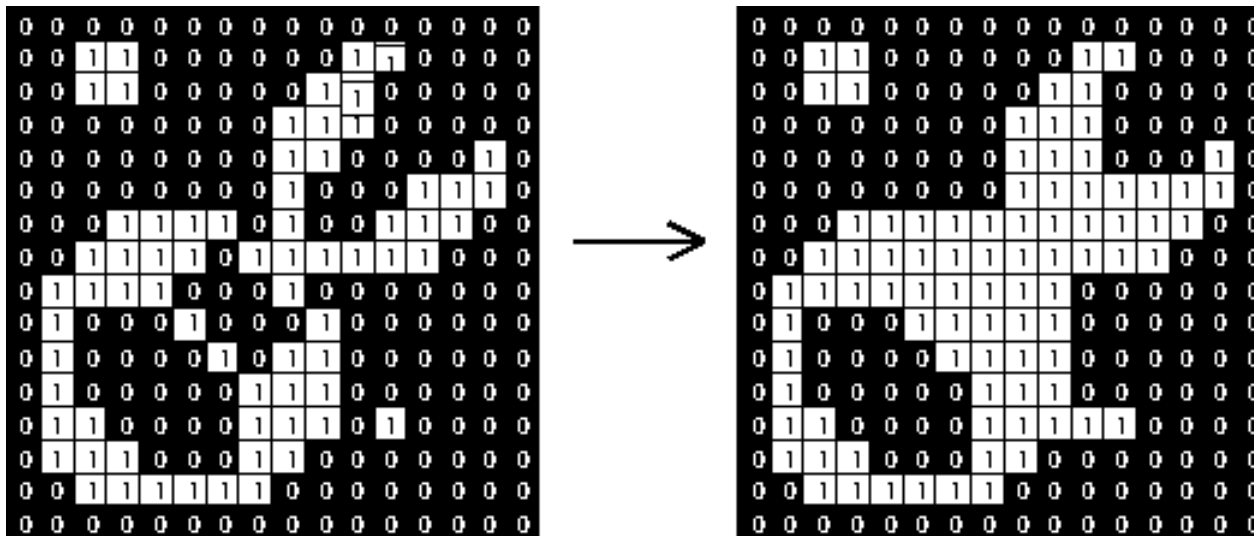
- Motivasi: Mengisi holes TETAPI tetap menjaga ukuran aslinya
- Opening = Dilation + Erosion
  - Gunakan SE yang sama
  - Hampir sama dengan dilasi tetapi tidak terlalu *destructive*
- Math:

$$f(x, y) \bullet SE = (f(x, y) \oplus SE) \ominus SE$$

- Closing adalah *idempotent*: operasi closing yang diulang-ulang tidak memberikan dampak yang berkelanjutan!

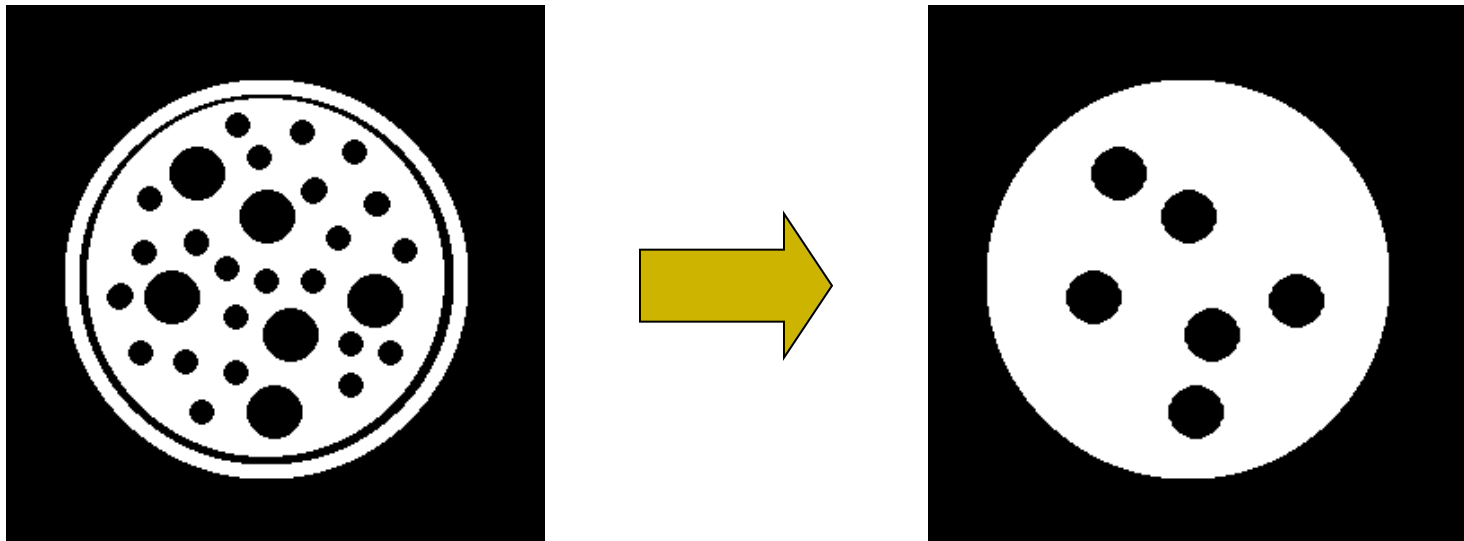
# Closing

- Structuring element: 3x3 square



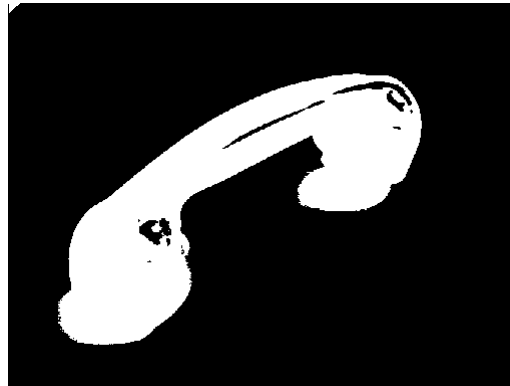
## Contoh Closing

- Operasi Closing dengan 22 piksel disc
- Menutupi holes yang kecil



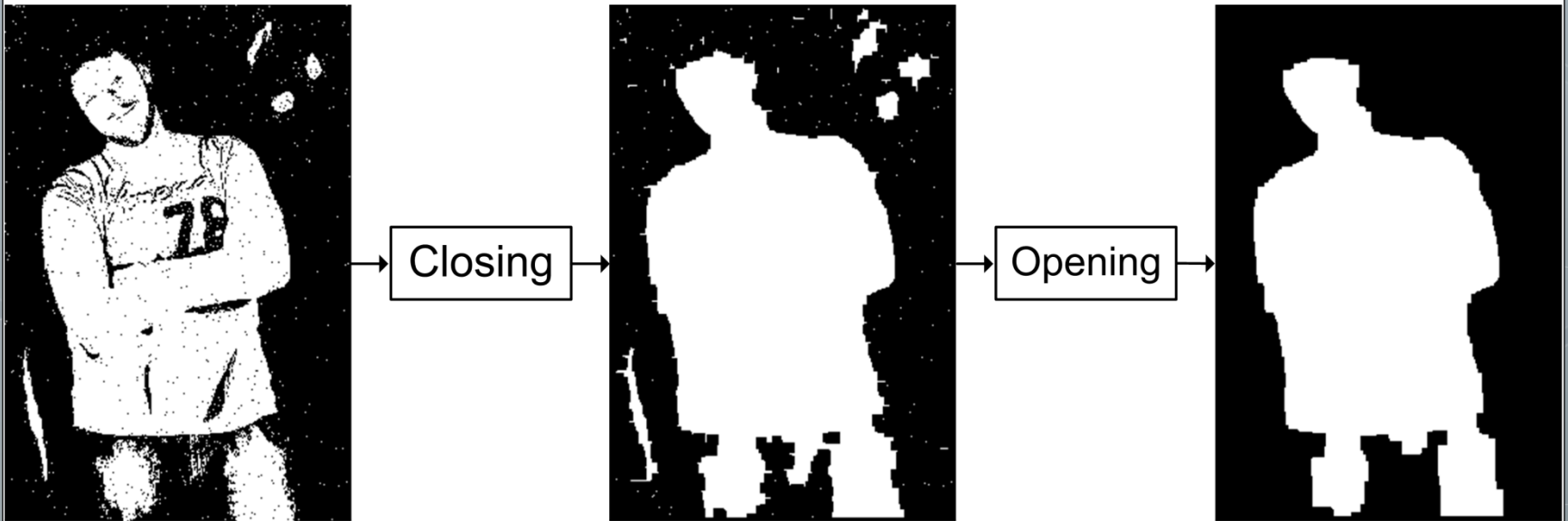
# Contoh Closing

- Improve segmentation
  1. Threshold
  2. Closing dengan ukuran 20 piksel disc

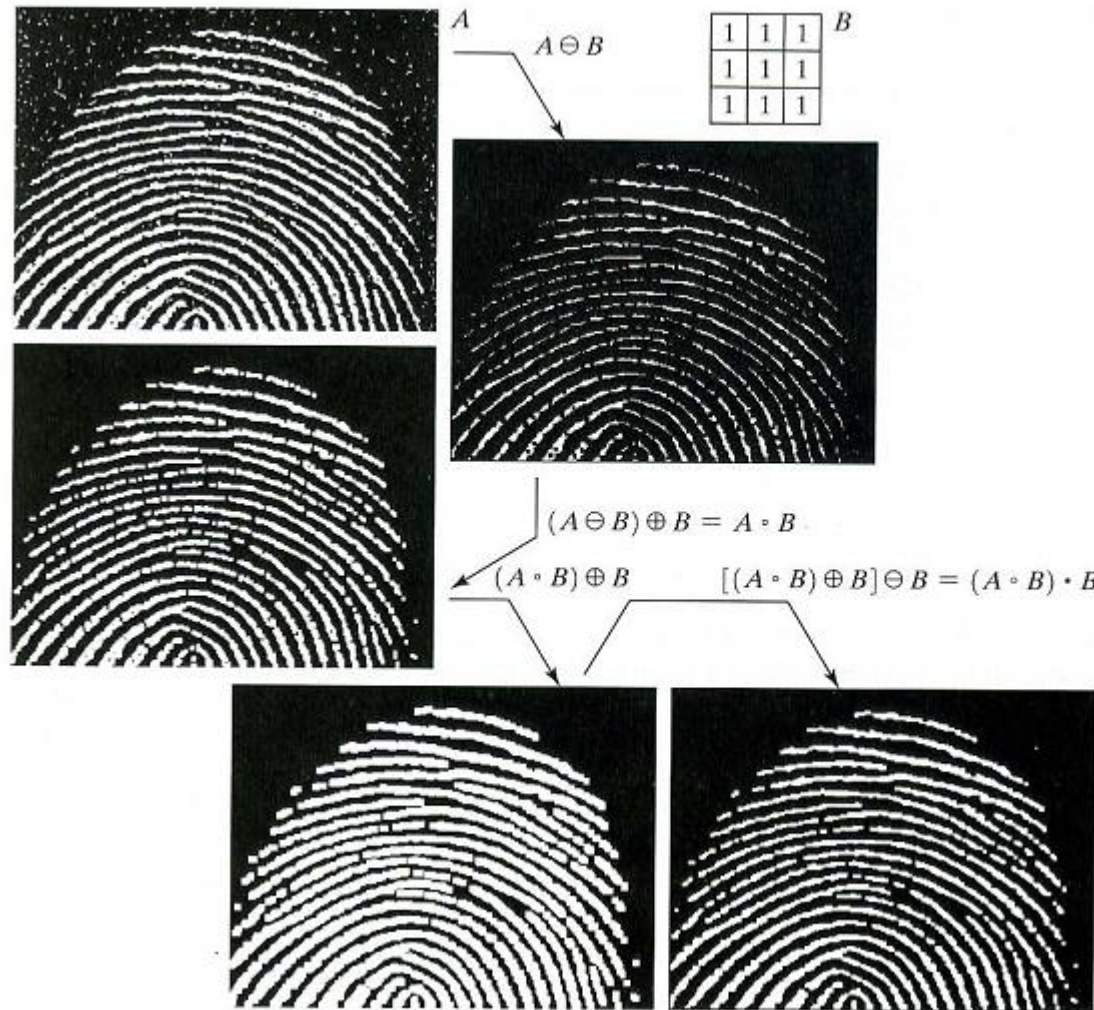


(show: blobs-holes, 1 x dilation, 1 x erosion)

# Kombinasi Opening dan Closing



# Kombinasi Opening dan Closing



a b  
c d  
e f

**FIGURE 9.11**

(a) Noisy image.  
(b) Structuring element.  
(c) Eroded image.  
(d) Opening of  $A$ .  
(e) Dilation of the opening.  
(f) Closing of the opening. (Original image for this example courtesy of the National Institute of Standards and Technology.)



# Ringkasan

- Morphology
- Fit and Hit operations
- Erosion (based on Fit): Make objects smaller
  - Separate objects, remove small objects (noise)
- Dilation (based on Hit): Make objects bigger
  - Remove holes in objects
- Compound operations
  - Finding the outlines of the objects
  - Opening (Erosion + Dilation)
    - As Erosion but less destructive
  - Closing (Dilation + Erosion)
    - As Dilation but less destructive

# Latihan

- Diberikan citra biner:
  - Dilation
  - Erosion
  - Closing
  - Opening
- Structuring element:

1	1	1
1	1	1
1	1	1

[illegible]

**Thank You !**