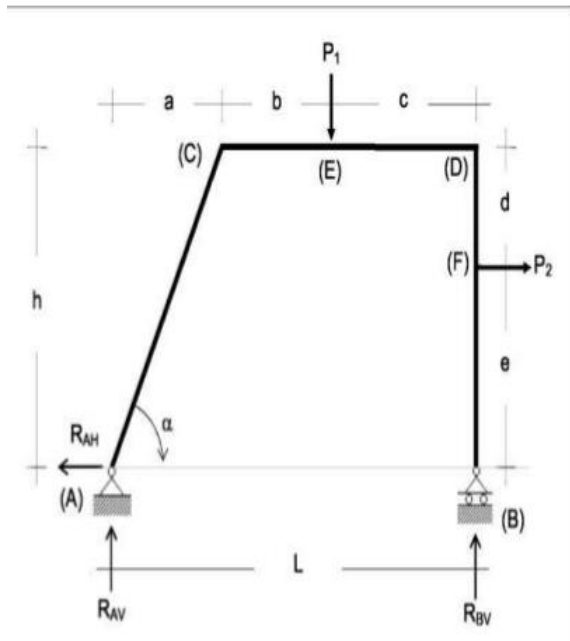


## PORTAL TIDAK SIMETRIS STATIS TERTENTU

### A Kolom miring sebelah, memikul muatan terpusat vertikal dan horisontal.



Diketahui : Konstruksi seperti tergambar.

$L=10\text{m}$ ,  $h=5\text{m}$ ,  $a=2\text{m}$ ,  $b=2\text{m}$ ,  $c=6\text{m}$ ,  $d=2\text{m}$ ,  $e=3\text{m}$ .  $P_1 = 5 \text{ ton}$ ,  $P_2 = 2 \text{ ton}$ .

Diminta : Hitung dan gambarkan M, D dan N pada seluruh bentang

## PENYELESAIAN

a. Reaksi Perletakan.

$$\begin{aligned}\sum M_B &= 0, \\ R_{AV} \cdot L - R_{AH} \cdot 0 - P_1 \cdot c + P_2 \cdot e &= 0 \\ R_{AV} &= P_1 \cdot c/L - P_2 \cdot e/L = 5 \cdot 6/10 - 2 \cdot 3/10 = 3 - 0,6 \\ R_{AV} &= + 2,4 \text{ ton (keatas)}.\end{aligned}$$

$$\begin{aligned}\sum M_A &= 0, \\ R_{BV} \cdot L + P_1 \cdot (a + b) + P_2 \cdot e &= 0 \\ R_{BV} &= P_1 \cdot (a+b)/L + P_2 \cdot e/L = 5 \cdot (2 + 2)/10 + 2 \cdot 3/10 = 2 + 0,6 \\ R_{BV} &= + 2,6 \text{ ton (keatas)}.\end{aligned}$$

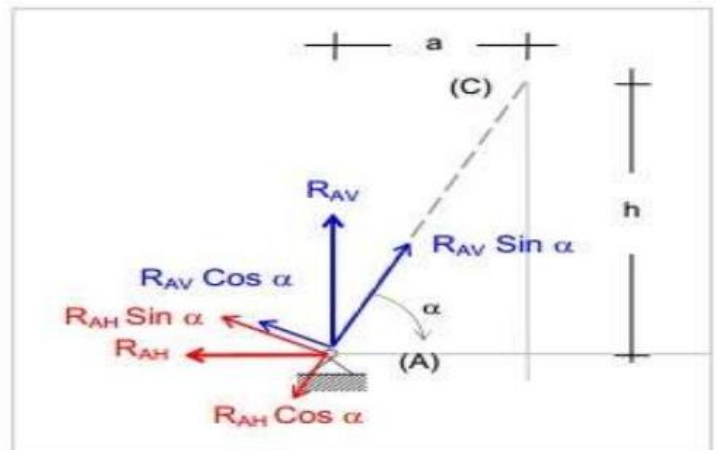
$$\begin{aligned}\sum H &= 0, \\ R_{AH} + P_2 &= 0 \\ R_{AH} &= P_2 = + 2 \text{ ton (kekiri)}.\end{aligned}$$

Kontrol :

$$\begin{aligned}\sum V &= 0, \\ R_{AV} + R_{BV} - P_1 &= 0 \\ 2,4 + 2,6 - 5 &= 0 \quad (\text{memenuhi}).\end{aligned}$$

- b. Gaya lintang.  
 $\alpha = \arctan(h/a) = \arctan(5/2) = 68^\circ 11' 55''$

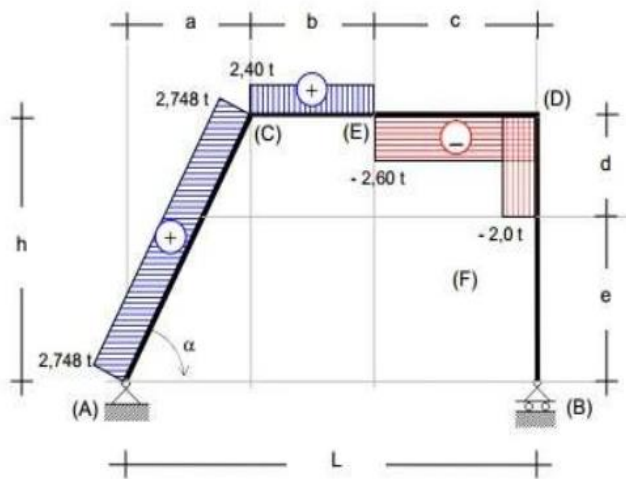
$$\begin{aligned} \text{DA-C} &= + R_{AH} \sin \alpha + R_{AV} \cos \alpha \\ &= 2 \cdot \sin(68^\circ 11' 55'') + 2,4 \cdot \cos(68^\circ 11' 55'') \\ &= + 1,857 + 0,891 \\ &= + 2,748 \text{ (ton)}. \\ \text{DC-E} &= + R_{AV} = + 2,4 \text{ (ton)}. \\ \text{DE-D} &= + R_{AV} - P_1 = 2,4 - 5 = -2,6 \text{ (ton)} \\ &= -R_{BV}. \\ \text{DD-F} &= -R_{AH} \\ &= -2 \text{ (ton)}. \end{aligned}$$



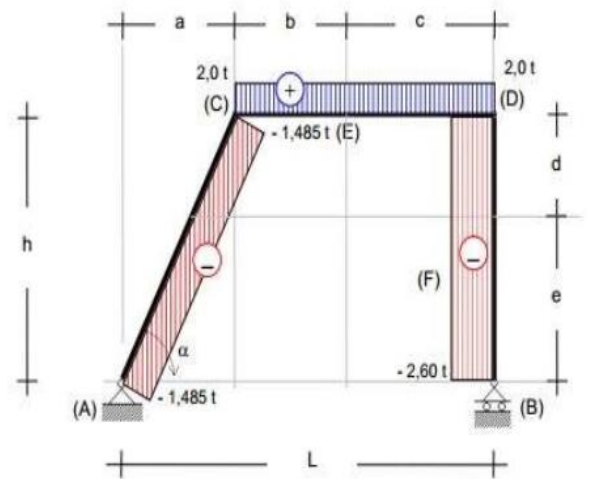
- c. Momen.  
 $M_A = 0$   
 $M_C = \pm R_{AH} \cdot h + R_{AV} \cdot a$   
 $= 2 \cdot 5 + 2,4 \cdot 2 = + 14,8 \text{ (t.m')}.$   
 $M_E = R_{AH} \cdot h + R_{AV} \cdot (a + b)$   
 $= 2 \cdot 5 + 2,4 \cdot (2 + 2) = + 19,6 \text{ (t.m')}.$   
 $M_D = R_{AH} \cdot h + R_{AV} \cdot L - P_1 \cdot c$   
 $= 2 \cdot 5 + 2,4 \cdot 10 - 5 \cdot 6 = + 4 \text{ (t.m')}.$   
 Atau,  
 $M_D = \pm P_2 \cdot d = + 2 \cdot 2 = + 4 \text{ (t.m')}.$   
 $M_F = R_{AH} \cdot e + R_{AV} \cdot L - P_1 \cdot c = 2 \cdot 3 + 2,4 \cdot 10 - 5 \cdot 6 = 0$   
 $M_B = 0$

- d. Gaya Normal.  
 $\alpha = 68^\circ 11' 55''$   
 $N_{A-C} = + R_{AH} \cos \alpha \pm R_{AV} \sin \alpha$   
 $= 2 \cdot \cos(68^\circ 11' 55'') - 2,4 \cdot \sin(68^\circ 11' 55'') = + 0,743 - 2,228$   
 $= - 1,485 \text{ ton (tekan)}.$   
 $N_{C-D} = + R_{AH} = + 2 \text{ ton (tarik)}.$   
 $N_{B-D} = - R_{BV} = - 2,6 \text{ ton (tekan)}.$

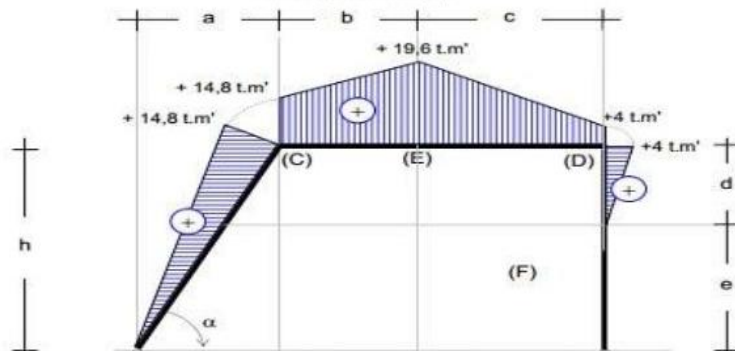
Bidang Gaya Lintang (D)



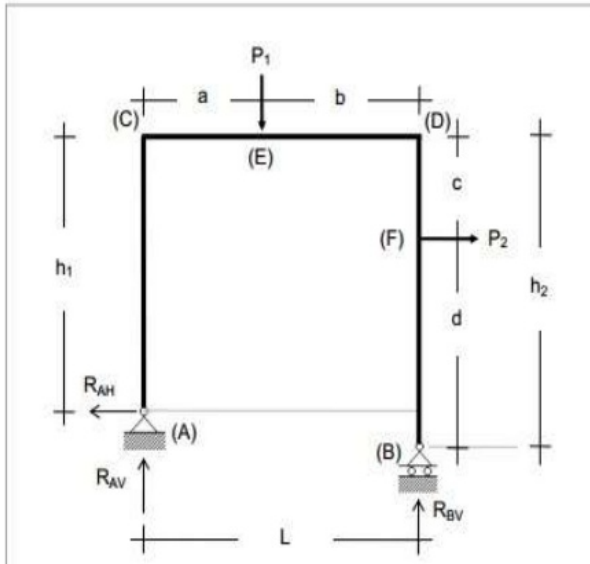
Bidang Gaya Normal (N)



Bidang Momen (M)



## B. Kolom tinggi sebelah, memikul muatan terpusat vertikal dan horisontal.



Diketahui :Konstruksi seperti tergambar.

$L = 10 \text{ m}$ ,  $h_1 = 5 \text{ m}$ ,  $h_2 = 6 \text{ m}$ ,  $a = 4 \text{ m}$ ,  $b = 6 \text{ m}$ ,  $c = 2 \text{ m}$ ,  $d = 4 \text{ m}$ .  $P_1 = 5 \text{ ton}$ ,  $P_2 = 2 \text{ ton}$ .

Diminta : Hitung dan gambarkan M, D dan N pada seluruh bentang!

## PENYELESAIAN

a. Reaksi Perletakan.

$$\sum H = 0,$$

$$R_{AH} + P_2 = 0$$

$$R_{AH} = -P_2 = -2 \text{ ton (kekiri)}.$$

$$\sum M_B = 0,$$

$$R_{AV} \cdot L - R_{AH} \cdot (h_2 - h_1) - P_1 \cdot b + P_2 \cdot d = 0$$

$$R_{AV} = \frac{P_1 \cdot b}{L} + \frac{R_{AH} \cdot (h_2 - h_1)}{L} - \frac{P_2 \cdot d}{L} \text{ (ton)}.$$

$$= \frac{5 \cdot 6}{10} + \frac{2 \cdot (6 - 5)}{10} - \frac{2 \cdot 4}{10}$$

$$= 3 + 0,2 - 0,8 \quad R_{AV}$$

$$= +2,4 \text{ ton (keatas)}.$$

$$\sum M_A = 0,$$

$$R_{BV} \cdot L + P_1 \cdot a + P_2 \cdot (h_1 - c) = 0$$

$$R_{BV} = \frac{P_1 \cdot a}{L} + \frac{P_2 \cdot (h_1 - c)}{L}$$

$$= \frac{5 \cdot 4}{10} + \frac{2 \cdot (5 - 2)}{10} = 2 + 0,6 \quad R_{BV}$$

$$= +2,6 \text{ ton (keatas)}$$

Kontrol :

$$\sum V = 0,$$

$$R_{AY} + R_{BV} - P_1 = 0$$

$$2,4 + 2,6 - 5 = 0 \dots (\text{memenuhi}).$$

b. Gaya lintang.

$$DA-C = + R_{AH} = + 2 \text{ ton.}$$

$$DC-E = + R_{AV} = + 2,4 \text{ ton.}$$

$$DE-D = + R_{AV} - P_1 = + 2,4 - 5 = - 2,6 \text{ ton. } DD-F = - R_{AH} = - 2 \text{ ton,}$$

atau

$$DD-F = - P_2 = - 2 \text{ ton.}$$

c. Momen.

$$M_A = 0$$

$$M_c = + R_{AV} \cdot h = + 2,4 \cdot 5 = + 12 \text{ t.m'}$$

$$M_E = + R_{AV} \cdot a + R_{AH} \cdot h + 2,4 \cdot 4 + 2 \cdot 5 = 19,6 \text{ t.m'}$$

$$M_D = + R_{AV} \cdot L + R_{AH} \cdot h - P_1 \cdot b$$

$$= 2,4 \cdot 10 + 2 \cdot 5 - 5 \cdot 6$$

$$= 24 + 10 - 30$$

$$M_D = + 4 \text{ t.m'}$$

Atau,

$$M_D = + P_2 \cdot c = + 2 \cdot 2 = + 4 \text{ t.m'}$$

$$M_F = + R_{AV} \cdot L + R_{AH} \cdot (h_1 - c) - P_1 \cdot b \text{ (t.m')} \text{ (dari kiri)}$$

$$= + 2,4 \cdot 10 + 2 \cdot (5 - 2) - 5 \cdot 6$$

$$= 24 + 6 - 30$$

d. Gaya Normal.

$$NA-C = R_{AV} = - 2,4 \text{ ton (tekan).}$$

$$NC-D = + R_{AH} = + 2 \text{ ton (tarik).}$$

$$NB-D = - R_{BV} = - 2,6 \text{ ton (tekan).}$$

